Compositional Physical Reasoning of Objects and Events from Videos

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Abstract— Understanding and reasoning about objects' physical properties in the natural world is a fundamental challenge in artificial intelligence. While some properties like colors and shapes can be directly observed, others, such as mass and electric charge, are hidden from the objects' visual appearance. This paper addresses the unique challenge of inferring these hidden physical properties from objects' motion and interactions and predicting corresponding dynamics based on the inferred physical properties. We first introduce the Compositional Physical Reasoning (ComPhy) dataset. For a given set of objects, ComPhy includes limited videos of them moving and interacting under different initial conditions. The model is evaluated based on its capability to unravel the compositional hidden properties, such as mass and charge, and use this knowledge to answer a set of questions. Besides the synthetic videos from simulators, we also collect a real-world dataset to show further test physical reasoning abilities of different models. We evaluate state-of-the-art video reasoning models on ComPhy and reveal their limited ability to capture these hidden properties, which leads to inferior performance. We also propose a novel neuro-symbolic framework, Physical Concept Reasoner (PCR), that learns and reasons about both visible and hidden physical properties from question answering. Leveraging an object-centric representation, PCR utilizes videos and the associated natural language to infer objects' physical properties without dense object annotations. Furthermore, It incorporates property-aware graph networks to approximate the dynamic interactions among objects. PCR also employs a semantic parser to convert questions into semantic programs, and a program executor to execute the programs based on the learned physical properties and dynamics. After training, PCR demonstrates remarkable capabilities. It can detect and associate objects across frames, ground visible and hidden physical properties, make future and counterfactual predictions, and utilize these extracted representations to answer challenging questions. We hope the proposed ComPhy dataset and the PCR model present a promising step towards more comprehensive physical reasoning in AI systems.

Index Terms—Physical Reasoning, Neuro-Symbolic Models, Hybrid Models.

1 INTRODUCTION

▲ **7** HAT causes apples to float in water while bananas sink? What is the underlying reason for magnets 3 attracting on one side and repelling on the other? Objects in nature frequently manifest complex properties, which de-5 lineate their interaction schema within the physical world. 6 For humans, deciphering these *intrinsic* physical properties often represents pivotal milestones in fostering a more pro-8 found and precise comprehension of nature. The majority 9 of these properties are intrinsic in nature, as they are not 10 readily apparent through objects' static visual attributes and 11 are only detectable from objects' interactions. Furthermore, 12 these properties influence object motion in a *compositional* 13 manner, where the causal relationships and mathematical 14 laws governing these properties can often be complex. 15

As depicted in Figure 1, various *intrinsic* physical prop erties, such as charge and inertia, often result in significantly
 divergent future trajectories. Objects bearing identical or op posite *charges* will exert either repulsive or attractive forces

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on one another. The resultant motion is not only related to 20 the magnitude of the charge each object possesses but also 21 to their respective signs, as illustrated in Figure 1-(a). Inertia 22 governs the degree of sensitivity of an object's motion to 23 external forces. In scenarios, where a massive object interacts 24 with a lighter one through attraction, repulsion, or collision, 25 the lighter object experiences more substantial alterations in 26 its motion relative to the trajectory of the massive object, as 27 depicted in Figure 1-(b). 28

Recent research has introduced a suite of benchmarks aimed at assessing and diagnosing machine learning systems across a range of physics-related settings [1]–[3]. These benchmarks present reasoning tasks involving intricate object motion and complex interactions, imposing significant challenges on existing models as they demand an understanding of the underlying physical dynamics to perform well. However, the majority of complexity in the motion trajectories facilitated by these environments arises from alterations or interventions in the initial conditions of the physical experiments. The impacts of objects' intrinsic physical properties, along with the distinct challenges they present, hold significant importance for further research.

However, it is non-trivial to construct a benchmark for compositional physical reasoning. A straightforward approach might involve adhering to the settings established in previous benchmarks [2], [4], wherein a model is required to observe a video and subsequently respond to questions regarding physical properties. Nevertheless, physical prop-47

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Fig. 1: Non-visual properties like mass and charge govern the interaction between objects and lead to different motion trajectories. a) Objects attract and repel each other according to the (sign of) charge they carry. b) Mass determines how much an object's trajectory is perturbed during an interaction. Heavier objects have more stable motion.

erties are intricate and often cannot be comprehensively 48 elucidated within the confines of a single video. Another 49 approach is to establish correlations between object ap-50 pearance and physical properties, such as designating all 51 red spheres as heavy, and subsequently posing questions 52 regarding their dynamics. Nonetheless, this design may 53 lead models to employ shortcuts by merely memorizing 54 appearances rather than comprehending the interconnected 55 physical properties. 56

In this paper, we present an extended version of the 57 ComPhy benchmark [5], with significant additions, includ-58 ing more diverse simulated scenes, real-world videos, and 59 new experimental settings. It centers on the comprehension 60 of object-centric and relational physics properties not read-61 ily discernible from visual appearances. Initially, ComPhy 62 presents a limited number of video examples featuring 63 dynamic interactions among objects. Models are tasked with 64 identifying the physical properties of objects and subse-65 quently answering questions pertaining to these properties 66 and their associated dynamics. 67

As depicted in Figure 2, the ComPhy is composed of 68 meta-train and meta-test sets, with each data point com-69 prising four reference videos and one target video. In each 70 set, the objects consistently possess the same intrinsic phys-71 ical properties across all videos. To facilitate the task, we 72 systematically ensure that each object in the query video 73 appears in at least one of the reference videos. Reasoning 74 on the ComPhy is challenging. First, models must infer both 75 the intrinsic and compositional physical properties of the 76 object set using only a limited number of video samples. 77 Moreover, they must predict video dynamics based on the 78 predicted physical properties. 79

To overcome the challenges in ComPhy, we introduce 80 Physical Concept Reasoner (PCR). Inspired by recent work 81 on neural-symbolic reasoning on images and videos [2], 82 [6], [7], our model is modularized with four disentangled 83 components: perception, physical property learning, physi-84 cal dynamics prediction, and symbolic reasoning. Our PCR 85 86 model can learn to infer objects' compositional and intrinsic 87 physical properties, predict their future dynamics, and make counterfactual imaginations by only watching videos and 88 reading question-answer pairs. 89

To summarize, this paper makes the following contribu-90 tions. First, we extend the original ComPhy benchmark [5] 91 by introducing new diverse simulated scenes and real-world 92 video data. It is based on a few-shot reasoning setting that 93 integrates physical properties (mass and charge), physical 94 events (attraction and repulsion), and their compositions. 95 Second, we introduce a new neural-symbolic framework 96 PCR, a modularized model that can infer objects' physical 97 properties and predict the objects' movements from watch-98 ing videos and reading question-answer pairs. Additionally, 99 we collect a real-video dataset to better assess the physical 100 reasoning capabilities of current models in real-world sce-101 narios. 102

Some preliminary results were presented in our earlier 103 ICLR 2022 paper [5]. In this manuscript, we significantly 104 extend that work in three aspects. First, we introduce a 105 Physical Concept Reasoner, PCR, to learn hidden physical 106 properties like *mass* and *charge* from video and language 107 efficiently without dense property supervision signals dur-108 ing training and perform reasoning in counterfactual and 109 predictive scenes. Second, besides the experiments in the 110 original data [8], we also simulate more diverse phys-111 ical scenes and collect real videos for physical reason-112 ing. We perform experiments in both synthetic and real 113 videos and analyze how the new proposed PCR works 114 and fails, while there are only experiments for synthetic 115 data in the original conference version. Third, we also eval-116 uate recent state-of-the-art large vision-language models 117 (LVLMs) [9], [10] on ComPhy, providing a more thorough 118 analysis. Our code, datasets, and models can be found at 119 https://physicalconceptreasoner.github.io. 120

The rest of the paper is organized as follows. Section 2 121 reviews the related datasets and models based on physical 122 reasoning, video question answering, and few-shot learn-123 ing. Section 3 introduces how we construct the dataset 124 and reduce its biases. Section 4 analyze how representative 125 baselines and the recent state-of-the-art models perform on 126 the ComPhy benchmark. Section 5 introduces the new PCR 127 model and its optimization mechanism. Section 6 summa-128 rizes the paper's contribution, discusses its limitations, and 129 suggests potential extension directions. 130

Dataset	Video	Question Answering	Diagnostic Annotation	Composition	Few-shot Reasoning	Physical Property	Counterfactual Property Dynamics	Evaluated on LVLM
CLEVR [11]	-	\checkmark	\checkmark	\checkmark	-	-	-	-
MovieQA [12]	\checkmark	\checkmark	-	\checkmark	-	-	-	-
TGIF-QA [13]	\checkmark	\checkmark	-	-	-	-	-	-
TVQA/ TVQA+ [14]	\checkmark	\checkmark	-	\checkmark	-	-	-	-
AGQA [15]	\checkmark	\checkmark	-	-	-	-	-	-
IntPhys [16]	\checkmark	-	\checkmark	-	-	\checkmark	-	-
PHYRE/ ESPRIT [17]	\checkmark	-	\checkmark	\checkmark	-	\checkmark	-	-
Cater [16]	\checkmark	\checkmark	\checkmark	\checkmark	-	-	-	-
CoPhy [3]	\checkmark	-	\checkmark	-	-	\checkmark	-	-
CRAFT [4]	\checkmark	\checkmark	\checkmark	\checkmark	-	-	-	-
CLEVRER [2]	\checkmark	\checkmark	\checkmark	\checkmark	-	-	-	-
Physion [18]	\checkmark	-	\checkmark	-	-	-	-	-
Physion++ [19]	\checkmark	-	\checkmark	-	-	\checkmark	-	-
ComPhy (ours)	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark

TABLE 1: Comparison between ComPhy and other visual reasoning benchmarks. ComPhy is a physical reasoning dataset with a wide range of reasoning tasks for physical property learning and corresponding dynamic prediction.

131 2 RELATED WORK

Physical Reasoning. Our research prominently aligns with 132 contemporary advancements in the domain of physical rea-133 soning benchmarks, as delineated by recent studies [4], [16], 134 [18]–[20]. PHYRE [1] and its variant, ESPRIT [17], establish 135 an environment where objects maneuver within a vertical 136 2D plane, influenced by gravitational forces. Each task 137 within this framework is tethered to a distinct goal state, and 138 the model seeks resolution by delineating initial conditions 139 conducive to achieving said state. Conversely, CLEVRER [2] 140 incorporates videos featuring multiple objects in motion, 141 colliding on a planar surface, and poses natural language 142 questions pertaining to the description, explanation, predic-143 tion, and counterfactual reasoning of the resultant collision 144 events. CoPhy [3] encompasses experimental trials involv-145 ing objects moving in 3D space under the influence of grav-146 ity, with a focal point on predicting object trajectories fol-147 lowing counterfactual interventions upon initial conditions. 148 CRIPP-VQA [21] introduces a challenge that emphasizes 149 reasoning over physical properties such as mass and friction 150 from a single video with simple primitive shapes, material 151 and colors. Our work builds upon the original ComPhy 152 dataset introduced in our prior work [5], extending it with 153 more diverse physical scenes and real-world videos, which 154 requires models to infer physical properties from a few 155 physical interactions in reference videos. Compared to other 156 previous datasets, ComPhy requires models to infer intrinsic 157 properties from a limited array of video examples and draw 158 dynamic predictions based on the identified properties. 159

Dynamics Modeling. Modeling the dynamics of physical 160 systems has long been a focal point of research. This issue 161 has been explored by some researchers through physical 162 simulations, drawing inferences regarding crucial system-163 and object-level properties via statistical methodologies 164 such as MCMC [22]–[24]. In contrast, others have pro-165 posed to directly ascertain the forward dynamics employing 166 neural networks [25]. Owing to their object- and relation-167 centric inductive biases and efficacy, Graph Neural Net-168 works (GNNs) [26] have been broadly applied in predict-169 170 ing forward dynamics across a diverse array of systems [27]–[30]. Our research combines the strengths of both ap-171 proaches: initially inferring the object-centric intrinsic phys-172 ical properties and subsequently predicting their dynamics 173

predicated on these intrinsic properties. **Video Question Answering.** Our research also pertains to the domain of video question answering, which responds to queries about visual content. Several benchmarks have been posited to address the task of video question answering, such as MarioQA [31], TVQA [32], and AGQA [15]. Nevertheless, these datasets primarily concentrate on comprehending human actions and activities rather than acquiring knowledge regarding physical events and properties, a competency crucial for robotic planning and control.

We summarize the differences between our extended ComPhy benchmark and other prior physical reasoning datasets in Table 1. Compared to our previous version [5], this work introduces more diverse simulated scenes and real-world videos. Notably, ComPhy remains the only dataset requiring models to infer physical properties from a sparse set of video examples, perform dynamics prediction, and answer compositional reasoning questions.

Few-shot Learning. Our research bears relevance to fewshot learning, which learns to classify images utilizing merely a few examples [33]–[36]. ComPhy mandates that models identify object property labels from a limited selection of video examples. Contrasting with the aforementioned works, reference videos in our approach do not furnish labels for objects' physical properties but exhibit more interactions among objects, thereby providing models with information to discern objects' physical properties.

3 DATASET

This section describes the dataset used in our benchmark. 202 We build upon our prior work ComPhy [5], originally in-203 troduced in ICLR 2022, and present a significantly extended 204 version. In addition to the synthetic split described in [5], 205 we enrich the synthetic dataset with more diverse physical 206 scenes and include a new real-world video dataset. First, 207 we introduce video details and the task setup in Section 3.1. 208 Subsequently, Section 3.2 delves into the different categories 209 of questions, while Section 3.3 explores the underlying 210 statistics and ensures balance. Finally, in Section 3.4, we 211 introduce how we build the real-world data set. 212

3.1 Videos

Objects and Events. Following [11], objects in ComPhy 214 are characterized by compositional appearance attributes, 215

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Fig. 2: Sample target video, reference videos and question-answer pairs from ComPhy.

including color, shape, and material. For ease of identifica-216 tion, each object in the videos is uniquely distinguishable 217 based on these three characteristics. The dataset incorpo-218 rates events such as *in*, *out*, *collision*, *attraction*, and *repulsion*. 219 The basic concepts in ComPhy are derived from these object 220 appearance attributes, events, and their compositionality. 221

Physical Properties. Previous benchmarks [2], [16] predom-222 inantly focused on visually perceptible appearance concepts 223 like color and collision, discernible in a single frame. In 224 225 contrast, our dataset, ComPhy, additionally explores the intrinsic physical properties of mass and charge, which are 226 not directly discernible from an object's static appearance 227 (Figure 1(a,b)). These properties are independent of visual 228 features and can interact, resulting in more intricate and 229 diverse dynamic scenarios. For simplicity, the dataset cat-230 egorizes objects into discrete mass groups (heavy / light) and 231 charge categories (positively / negatively charged / uncharged). 232 While introducing additional continuous parameters like 233 bounciness and friction is possible, the complexity could 234 render the dataset overly intricate and hinder intuitive 235 property inference from people. 236

Video Generation. Each target video designated for 237 238 question-answering encompasses 3 to 5 objects, integrating a random compositionality of appearance attributes and 239 physical properties. The videos are standardized to a du-240 241 ration of 5 seconds, with an extended simulation of the 6-th

and 7-th seconds specifically for annotating questions for 242 future prediction. 243

As in our prior work [5], the synthetic videos are gen-244 erated in a two-step process using the Bullet physics engine and rendered via Blender. In the first step, we employ the Bullet physical engine [37] to simulate the movements of objects and their interactions with one another. Since Bullet does not officially support the effect of electronic charges, we add external forces between charged objects, 250 whose values are inversely proportional to the square of the 251 objects' distance, to simulated Coulomb forces. We assign a 252 mass value of 1 to the *light* objects and a mass value of 5 to 253 the *heavy* objects. We manually ensure that every reference 254 video includes at least one interaction, such as collision, 255 attraction, or repulsion, among objects, to provide sufficient 256 information for inferring physical properties. Every object in 257 the target video must appear in the reference videos at least 258 once. The simulated object movements are then transmitted 259 to Blender [38] for high-quality image sequences. 260

Task Setup. It presents a non-trivial challenge to design 261 an evaluative framework that accurately assesses a model's 262 capacity for physical reasoning because physical proper-263 ties are not discernible within a static frame. A simplistic 264 approach would involve associating physical attributes di-265 rectly with object appearances like "The red object is heavy", 266 "The yellow object is light" and then asking "What would hap-267

pen if they collide?" However, this setting is flawed, as it fails 268 to ascertain whether the model genuinely comprehends the 269 physical properties or merely relies on memorizing visual 270 cues. An ideal setup would demand a model to demonstrate 27 human-like discernment of objects' properties from their 272 273 motion and mutual interactions within dynamic scenes, and 274 subsequently formulate relevant dynamic predictions.

To achieve this goal, We introduce a meta-framework 275 for physical reasoning that pairs a target video with a 276 limited set of reference videos, enabling models to infer 27 physical properties. Questions are then formulated regard-278 ing these properties and underlying dynamics, as illustrated 279 in Figure 2. Thus, each collection includes a target video, 280 four reference videos, and numerous inquiries related to 281 the target video. Notably, all objects within each collection maintain consistent visual attributes, including color, shape, 283 and material, as well as intrinsic physical properties, specif-284 285 ically mass and charge.

Reference Videos. To enrich the visual content for physical 286 property inferring, we supplement each target video with 287 four reference videos. From the target video, we select 2 to 3 288 objects, assign them different initial velocities and positions, 289 and orchestrate interactions such as attraction, repulsion, 290 or collision. The reference videos, though lasting 2 seconds 291 each for scalability, follow the same generation criteria as 292 the target videos. These supplementary interactions help models deduce physical properties; for example, observing 294 repulsion in Reference Video 1 of Figure 2 indicates that 295 *object 1* and *object 2* possess the same electrical charges. 296

3.2 Questions 297

Inspired by the previous datasets [2], [11], we propose a 298 question engine capable of generating questions that test 299 factual, predictive, and counterfactual reasoning abilities. 300

Queries. Factual questions are open-ended, requiring concise 301 answers in the form of a single word or short phrase, and assess a model's understanding and reasoning about 303 objects' physical properties, visual attributes, events, and re-304 lationships. Building upon existing benchmarks [2], [4], our 305 dataset (ComPhy) introduces novel and challenging factual 306 questions focused specifically on the physical properties of 307 charge and mass (See Figure 2 (I)). Predictive and counter-308 factual questions, conversely, adopt a multiple-choice for-309 310 mat that critically evaluates the plausibility of each provided answer option. *Predictive questions* require models to analyze 311 objects' physical properties and dynamics to forecast events 312 in future video frames. Counterfactual questions investigate 313 hypothetical scenarios where an object's physical properties 314 (e.g., charge or mass) are altered, focusing on their impact 315 on object dynamics (See Figure 2 (II)). This methodology 316 contrasts with prior research [2], [16] that centered on object 317 removal, emphasizing the divergent implications of chang-318 ing physical properties for predicting motion instead. 319

Templates. We present typical question templates in Ta-320 ble 2. Examining the table reveals that these novel question 32 templates incorporate diverse symbolic operators associated 322 with physical properties. For example, phrases such as 323 "heavy moving spheres" and "charged cubes" demand that models deduce the values of objects' physical properties. 325 For counterfactual questions, we introduce novel condi-326 327 tions, such as "If the cyan object were uncharged" and "If

Type Template and Example
CUN1 If the <i>SA</i> were <i>MP</i> , <i>Q</i> ? If the sphere were lighter, which event would not happen?
CUN2 If the <i>SA</i> were <i>CP</i> , <i>Q</i> ? If the cube were uncharged, which event would happen?
Mass1 Is the <i>DA1 SA1</i> heavier than the <i>DA2 SA2</i> ? Is the blue sphere heavier than the gray cube?
Mass2 Is the <i>DA1 SA1</i> lighter than the <i>DA2 SA2</i> ? Is the blue sphere lighter than the gray cube?
CHR1 Are the <i>DA1 SA1</i> and the <i>DA2 SA2</i> oppositely charged? Are the blue sphere and the purple sphere oppositely charged?
CHR2 Are the <i>DA1 SA1</i> and the <i>DA2 SA2</i> with the same type of charge? Are the cube and the cylinder with the same type of charge?
CHR3 What are the <i>Hs</i> of the two objects that are charged? What are the colors of the two objects that are charged?
Query What is the <i>H</i> of the <i>DA SA</i> that is <i>PA</i> ? What is the color of the moving cylinder that is heavy?
Exist Are there any <i>PA DA SA TI</i> ? Are there any charged moving cube when the video ends?
Count How many PA DA SA are there TI? How many heavy stationary spheres are there?

TABLE 2: Typical question templates and examples in Com-Phy. SA denotes static attributes like "red"; DA denotes dynamic attributes, "moving"; MP denotes mass attributes like "heavier"; Q denotes question phrases like "which of the following would happen"; CP denotes charge attributes like "uncharged"; H denotes visible concepts like "material"; PA denotes physical attributes like heavy and charged; TI denotes time indicators like "when the video ends".

the sphere were lighter". These conditions are designed to 328 enable reasoning about the dynamics when a particular 329 object possesses an alternative physical property. 330

3.3 Balancing and Statistics

In total, ComPhy features 8,000 training sets, 2,000 for 332 validation, and 2,000 for testing, with a total of 41,933 333 factual, 50,405 counterfactual, and 7,506 predictive questions 334 constituting 42%, 50%, and 8% of the dataset, respectively. 335 For simplicity, video sets will include a pair of charged 336 objects only if charged objects are already present, and 337 similarly, a video will contain a heavy object or none at all. 338 We ensure that these few video examples are sufficiently 339 informative to answer questions based on the questions' 340 programs and the properties and interaction annotations 341 in the videos. Specifically, for questions comparing mass 342 or establishing charge relations, we meticulously confirm at 343 least one interaction exhibited between the relevant objects. 344

3.4 **Real-World Datasets**

As shown in Fig. 3, we collect a new real-world video 346 dataset to further estimate the capabilities of physical rea-347 soning models. The construction of this dataset involves two 348 key stages: real video collection and question annotation. 349 **Real Video Collection.** We capture a dataset consisting of 350 492 real-world videos using the iPhone's SLO-MO feature, 351 which records high-definition slow-motion footage at 240 352 frames per second. These videos are organized into 123 353 sets, with 60 sets designated for training and 20 sets for 354

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Fig. 3: Samples of real data. We collect real objects of different mass values and magnetism for extensive experiments, which have a significant effect on objects' motion and interaction.

validation. Each set comprises one target video featuring 3-355 4 objects interacting and 3 associated reference videos con-356 taining 2-3 objects each. This design mirrors the simulated 357 video split, focusing on object interactions characterized 358 by attributes like color (red, brown, grey), shape (cylinder, 359 cube, sphere), magnetism (neutral, attractive, repulsive), 360 and mass (heavy and light) in physical world environment. 361 **Question Annotations.** The static attributes, physical prop-362 erties, and events in each video are initially annotated by an 363 annotator and subsequently checked by another to ensure 364 their correctness. We utilize a question engine similar to 365 the one used in the simulated split to generate diverse 366 questions, including counterfactual, predictive, and various 367 property-based inquiries. The engine randomly selects from 368 predefined templates and incorporates video annotations to 369 create questions that explore various aspects of physical interaction, such as magnetism's effect on dynamics, the 371 influence of mass, and the objects' static attributes. We 372 373 collect 1,068 questions in total, including 776 for physical properties, 134 for counterfactual reasoning, and 158 for 374 predictive future events. We provide more details on real-375 world videos in the supplementary material. 376

377 4 EXPERIMENTS

In this section, we assess baseline models and conduct an in-depth analysis to comprehensively study ComPhy.

380 4.1 Baselines

We assess multiple baseline models on ComPhy, as displayed in Table 3. These baselines fall into four categories: bias-analysis models [39], video question answering models [40], [41], compositional reasoning models [42], [43], and large vision-language foundation models [9], [10], [44]. For a comprehensive comparison, we additionally introduce variant models that leverage both the target video and reference videos.

Biased Analysis Models. The first category of models is
 bias analysis models. These models predict answers without

relying on visual input and aim to scrutinize the language 391 bias present in ComPhy. In particular, the Random model 392 randomly selects answers based on the question type and 393 requires no training. The **Frequent** model selects the most 394 frequently occurring answer in the training set for each 395 question type, which requires no training phase. **Blind**-396 **LSTM** employs an LSTM [39] to encode the question and 397 predict the answers without visual input; it is trained solely 398 on the question-answer pairs from the dataset's training 399 split to isolate language bias. 400

Visual Question-Answering Models. The second category 401 of models encompasses visual question-answering models. 402 These models answer questions based on input videos and 403 questions. The CNN-LSTM model [45] is a simple question-404 answering model. It employs a ResNet-50 [46] to extract 405 frame-level features, averaging them across the time dimen-406 sion. We encode questions using the final hidden state from 407 an LSTM [39]. The visual features and question embedding 408 are concatenated to make answer predictions with two fully-409 connected layers. HCRN [41] is a widely adopted model 410 that hierarchically models visual and textual relationships. 411 Both CNN-LSTM and HCRN were trained (or fine-tuned, if 412 using pre-trained components like ResNet) on the training 413 split until convergence on the validation set. 414

Visual Reasoning Models. The third category, visual rea-415 soning models, includes MAC [42], which decomposes 416 visual question answering into several attention-focused 417 reasoning steps, making predictions based on the hidden 418 output of the final step. In contrast, ALOE [43] capitalizes 419 on transformers [47] and object-centric representation to 420 deliver cutting-edge results on CLEVRER. We use MONet 421 [48] to extract visual representation for ALOE. Similar to the 422 VQA models, both MAC and ALOE were trained (or fine-423 tuned from general pre-trained weights where applicable) 424 on the dataset's training split. 425

Large Vision Language Models. The final model category 426 is large vision language models [9], [10], [44], which have 427 been trained on massive vision-language data and shown 428 excellent performance on both language understanding and 429 visual question answering. For ALPRO, we fine-tune the 430 model with ComPhy's training set until they achieve sat-431 isfactory results on the validation set. For GPT-4V and 432 Gemini, we evenly sample a fixed number of frames from 433 each target video as visual input, pairing them with corre-434 sponding questions and a carefully crafted text prompt to 435 guide the model in generating formatted answers. 436

Baselines with Reference Videos. We also introduce variations of existing baseline models that utilize both the target video and reference videos as input. We enhance **CNN-LSTM**, **MAC**, and **ALOE** to create **CNN-LSTM** (**Ref**), **MAC** (**Ref**), and **ALOE** (**Ref**) by incorporating the features of both reference videos and the target video as visual input. We uniformly sample 25 frames from each target video and 10 frames from each reference video.

Training and Evaluation Fairness. To ensure fair comparison, all models that underwent training or fine-tuning (**Blind-LSTM, CNN-LSTM, HCRN, MAC, ALOE, ALPRO,** and the 'Ref' variants) were trained on the same training split. We employed consistent hyperparameter tuning strategies (where applicable) and evaluated all models under identical conditions on the validation/test splits using

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Methods	Factual	Prec per opt.	lictive per ques.	Counte per opt.	erfactual per ques.
Random	29.7	51.9	22.6	49.7	9.1
Frequent	30.9	56.2	25.7	50.3	8.7
Blind-LSTM	39.0	57.9	28.7	55.7	12.5
CNN-LSTM [40]	46.6	59.5	29.8	58.6	14.6
HCRN [41]	47.3	62.7	32.7	58.6	14.2
MAC [42]	68.6	60.2	32.2	60.2	16.0
ALOE [43]	54.3	65.9	35.2	65.4	20.8
CNN-LSTM (Ref) [40]	41.9	59.6	29.4	57.2	12.8
MAC (Ref) [42]	65.8	60.2	30.7	60.3	14.3
ALOE (Ref) [43]	57.7	67.9	37.1	67.9	22.2
ALPRO [44]	45.2	56.9	27.2	53.7	14.4
GPT-4V [9]	42.2	60.7	47.1	51.1	8.9
Gemini [10]	37.7	46.5	22.7	49.2	6.3
Human Performance	90.6	88.0	75.9	80.0	52.9

TABLE 3: Evaluation of physical reasoning on ComPhy. Human performance is based on sampled questions. See Section 4.2 for more details. **Red** text and **blue** text indicate the first and the second best results.

the specified metrics. The zero-shot evaluation of GPT-4V
and Gemini is reported separately and interpreted in light
of their lack of dataset-specific fine-tuning.

We employ the conventional accuracy metric to assess the performance of various methods. In the case of multiplechoice questions, we provide both per-option accuracy and per-question accuracy. A question is deemed correct if the model answers all of its options correctly.

460 4.2 Evaluation on physical reasoning

The question-answering results of various baseline models are shown in Table 3. Notably, there exist discrepancies in the relative performances of models across different kinds of questions, which suggests that diverse reasoning skills are necessitated by the questions in ComPhy.

Factual Reasoning. To address factual questions in Com-466 Phy, models must identify visual attributes, analyze motion 467 trajectories, and infer physical properties of objects. The 468 results indicate that the "blind" models, namely Random, Frequent, and Blind-LSTM, perform significantly poorly 470 on ComPhy compared to other models integrating visual 471 context and linguistic information. Additionally, we observe 472 that video question-answering models and pre-trained large 473 vision language models exhibit lower performance com-474 pared to visual reasoning models like MAC and ALOE. We 475 attribute this discrepancy to the fact that they are typically 476 tailored for tasks such as object classification, action recogni-477 tion, and activity understanding rather than understanding 478 physical events in ComPhy. Among these, MAC outper-479 forms the rest baselines when answering factual questions, 480 underscoring the effectiveness of its compositional attention 481 mechanism and iterative reasoning processes. 482

Dynamcis Reasoning. A notable feature of ComPhy is its demand for models to generate counterfactual and future dynamic predictions by leveraging their identified physical properties to address posed questions. Among all the baseline models, we have observed that **ALOE (Ref)** consistently attains the highest performance levels in tasks involving counterfactual and future reasoning. We posit that this superior performance is attributable to the utilization of selfattention mechanisms and self-supervised object masking techniques, enabling the model to effectively capture spatiotemporal visual context and imagine counterfactual scenarios for answering questions.

Reasoning with Large Vision-Language Models. We also 495 evaluate the performance of the recent large vision-language models, ALPRO, Gemini and GPT-4V on ComPhy, which 497 were pre-trained on massive image/video-text pairs from the internet. Despite their strong performance on traditional visual question-answering benchmarks such as GQA [49], 500 VQAv2 [45], MSRVTT-QA [50] and MSVD-QA [50], all of 501 them underperform on ComPhy. The inferior performance 502 of large vision-language models (LVLMs) is attributed to 503 a gap in their training. These models are pretrained on 504 internet data, which primarily focuses on object categories 505 and semantic relations, lacking emphasis on physical com-506 monsense. ComPhy underscores its value in addressing the 507 gap and complementing the missing physical commonsense 508 in existing visual question-answering benchmarks. 509

Reasoning with Reference Videos. The results reveal that 510 CNN-LSTM (Ref) and MAC (Ref) perform comparably or 511 slightly worse than their original counterparts, CNN-LSTM 512 and MAC. While ALOE (Ref) shows a modest improvement 513 over ALOE, the variant models do not exhibit substantial 514 improvements when incorporating the reference videos as 515 supplementary visual input. This phenomenon is likely due 516 to these models' primary training on extensive datasets 517 comprising videos and question-answer pairs, hindering 518 their adaptability to ComPhy's novel context, which ne-519 cessitates discerning new compositional visible and hidden 520 physical properties from a limited number of examples. 521

Human Performance. To evaluate human performance in 522 ComPhy, 14 participants with a basic understanding of 523 physics and proficiency in English were tasked. After an 524 initial warm-up through a series of demonstration videos 525 and questions to confirm their comprehension of events and 526 physical properties, they were assigned to answer 25 diverse 527 question samples from ComPhy. Their accuracy rates are 528 as follows: 90.6% for factual questions, 88.0% for predictive 529 questions per option, 80.0% for counterfactual questions per 530 option, 75.9% for predictive questions per question, and 531 52.9% for counterfactual questions per question. 532

Reasoning in the Real World. We evaluated the perfor-533 mance of various models on our collected real-world dataset 534 by fine-tuning each model on the dataset's training split 535 and evaluating on the validation split (see Table 4). Results 536 indicate that ALOE achieves the highest accuracy on factual 537 questions (61.6%), consistent with its strong performance 538 observed in simulated scenarios. Notably, MAC shows a 539 balanced performance across all question types, particularly 540 excelling in predictive questions (57.1% per question accu-541 racy). Interestingly, state-of-the-art general-purpose vision-542 language models such as GPT-40-mini and Gemini sig-543 nificantly underperform compared to specialized models, 544 reflecting substantial limitations in their ability to reason 545 about physical interactions in real-world contexts. The sub-546 stantial gap between human performance (exceeding 88% 547 across all categories) and the evaluated models underscores 548 the complexity and challenge of physical reasoning tasks. 549



Fig. 4: The perception module detects objects' location and visual appearance attributes. The physical property learner learns objects' properties based on detected object trajectories. The dynamic predictor predicts objects' dynamics in the counterfactual scene based on objects' properties and locations. Finally, an execution engine runs the program parsed by the language parser on the predicted dynamic scene to answer the question.

Methods	Factual	Prec per opt.	lictive per ques.	Counte per opt.	erfactual per ques.
Random	7.6	50.0	25.0	50.9	20.8
Frequent	41.7	53.6	28.7	50.0	23.9
Blind-LSTM	50.6	61.5	46.0	51.9	32.2
CNN-LSTM [40]	55.6	64.2	47.3	50.9	33.3
HCRN [41]	51.9	62.5	53.5	50.9	32.1
MAC [42]	58.9	60.9	57.1	52.8	35.8
ALOE [43]	60.8	60.6	42.4	47.1	28.7
CNN-LSTM (Ref) [40]	49.0	64.3	41.3	50.0	26.3
MAC (Ref) [42]	56.4	56.2	46.4	51.4	34.9
ALOE (Ref) [43]	61.6	61.4	42.8	51.6	32.1
ALPRO [44]	50.9	55.3	39.2	49.7	29.2
GPT-40-mini [9]	42.6	49.6	23.2	47.5	26.0
Gemini [10]	32.5	57.7	23.1	52.1	29.8
Human Performance	90.0	95.0	90.0	94.4	88.9

TABLE 4: Evaluation of physical reasoning on the real video. Human performance is based on sampled questions.

550 5 MODELS

551 5.1 Model

In this section, we present Physical Concept Reasoner 552 (PCR), a new physical reasoning model. It aims to com-553 prehend objects' visible properties, infer hidden physical 554 properties and events, and image corresponding physical 555 dynamics by observing the videos and responding to the 556 associated questions. Compared with our preliminary mod-557 els [5], [8], it is able to infer hidden physical properties and 558 predict corresponding property-based dynamics without 559 explicit dense property annotations. 560

PCR can be factorized into different functional modules for physical reasoning in videos. As shown in Fig. 4, the

model consists of five major modules: (1) video perceiver, (2) 563 visible property grounder, (3) physical property inferencer, 564 (4) property-based dynamic predictor, and (5) differentiable 565 symbolic executor. When provided with a target video 566 alongside four reference videos and a query, PCR employs 567 a video perceiver to detect objects' spatial locations across 568 frames and all videos. Subsequently, their trajectories are 569 processed by the physical property inferencer to deduce 570 their properties. Leveraging these data, the dynamic predic-571 tor forecasts object movements based on their physical traits. 572 Lastly, a differentiable executor executes the program gen-573 erated by a language parser [6], [47], utilizing the predicted 574 object motions to answer the query. Note that the object-575 centric representation and outputs of various modules are 576 maintained in a differentiable manner, enabling direct op-577 timization of each module through backpropagation when 578 answering video-related questions. 579

5.1.1 Video Perceiver

Object Tracking and Alignment. Given a target video and 581 4 reference videos, the video perceiver in PCR is responsible 582 to track objects in every video and align them across differ-583 ent videos. The first step is to track objects in the videos. At 584 the *t*-th frame, our model first applies a regional proposal 585 network [51], [52] to detect all objects $\{b_i^t\}_{i=1}^{N_t}$, where N_t 586 denote the object proposal number. The video perceiver 587 then get a set of object trajectories $\{o_n\}_{n=1}^N$, where N is 588 the number of object trajectories, $o_n = \{b^t\}_{t=1}^T$ and T is 589 the number of frames. Similar to [5], [53], we first define 590 the connection score $s_{cnn}(b_i^t, b_j^{t+1})$ between two proposals 591 b_i^t and b_i^t in connective frames as 592

$$s_{cnn}(b_i^t, b_j^{t+1}) = s_c(b_i^t) + s_c(b_j^{t+1}) + \operatorname{IoU}(b_i^t, b_j^{t+1}), \quad (1)$$

where $s_c(b_i^t)$ is the confidence score predicted by the re-593 gion proposal network and IoU denotes the interaction 594 over union between two proposals. We define the connec-595 tion score of a candidate object trajectory $o_n = \{b_n^t\}_{t=1}^T$ as 596 $E(o_n) = \sum_{t=1}^{T-1} s_{cnn}(b_n^t, b_n^{t+1})$. We select the set of object trajectories $\{o_n\}_{n=1}^N$ with the highest connection scores and 597 598 solve the problem with a linear sum assignment [54]. We 599 then align objects in reference videos to the target videos 600 with the predicted static visual attributes, color, shape, and 601 material. Objects in reference videos are assigned to objects 602 in the target video that has the most similar predicted labels. 603 Object-Centric Representation. We use a set of object-604 centric features to represent the videos for physical reason-605 ing. Specifically, we compute the averaged visual regional 606 features ($\mathbf{f}_n^v \in \mathbf{R}^{\mathbf{D}_v}$) from the faster-RCNN [52] for static 607 visual appearance attributes like shape, color and material, 608 where D_v equals to 512 and is the regional feature's di-609 mension from ResNet-34. We adopt the temporal trajectory 610 features ($\mathbf{f}_n^t \in \mathbf{R}^{\times \mathbf{D}_t}$) for predicting temporal concepts like 611 in and out, where $D_s = T \times 4$ is the concatenation of the 612 object location b_n^t across all T frames. Since we can only 613 infer objects' physical property values from their movement 614 and interaction, we use a set of aligned trajectory features 615 for physical property inference. For the *n*-th object in the 616 target video, we represent it with \mathbf{p}_n and $\{\mathbf{p}_{n,r}\}_{r=1}^{\hat{R}}$, where 617 $\mathbf{p}_{n,r}^t$ and $\mathbf{p}_{n,r}$ are the concatenation of the object coordinates 618 (x_n^t, y_n^t) along all T frames in the target video and the r-619 th reference video. R equals to 4 and is the number of the 620 reference videos. We add all the objects without appearance 621 in the specific reference videos with zero vectors. 622

We use the interaction feature $(f_{i,j,t}^{int} \in \mathbf{R}^{D_{int}})$ for 623 prediction the the collision event between the *i*-th and the 624 *j*-th objects at the *t*-th frame. we define $f_{i,j,t}^{int} = f_{i,j,t}^{u} ||f_{i,j,t}^{loc}|$ 625 where $f_{i,j,t}^{u}$ is the ResNet feature of the union region of the 626 *i*-th and *j*-th objects at the *t*-th frame and $f_{i,j,t}^{sp}$ is a spatial 627 embedding for correlations between bounding box trajectories. We define $f_{i,j,t}^{sp} = \text{IoU}(s_{i,t}, s_{j,t})||(s_{i,t} - s_{j,t})||(s_{i,t} \times s_{j,t})$, 628 629 where $s_{i,t} = ||_{k=t-2}^{t+2} b_i^k$ is the concatenated segment of the 630 *i*-th object centering at the *t*-th frame. It concatenates the 631 intersection over union (IoU), difference (-), and multiplica-632 tion (\times) of the normalized trajectory coordinates for the *i*-th 633 and *j*-th objects centering at the *t*-th frame. For the collision 634 event in the future and counterfactual scenes, we predict the 635 collision event based on the $f_{i,j,t}$ only since there is no RGB 636 image for extracting the $f_{i,j,t}^u$ feature. 637

638 5.1.2 Visible property grounder

The visible property grounder grounds objects' visible prop-639 erties like color, shape, and collision onto the objects ex-640 tracted by the video perceiver. PCR accomplishes this by 641 aligning the representations of objects and events with 642 learned concept embeddings in PCR. For example, to predict 643 the *n*-th object is *red* or not, we use a confidence score 644 s_n^{red} . We define $s_n^{red} = \left[\cos(c^{red}, m_{sa}(f_n^v)) - \delta\right]/\lambda$, where 645 c^{red} is a vector, representing the concept *red*, m_{sa} is a 646 fully-connected layer, mapping the object feature f_n^v to the 647 color space. cos calculates the cosine similarity between 648 the two vectors. δ and λ_{sa} are constant scalars, controlling 649 the value range of s_{red} . Similarly, we predict two objects collide at the *t*-th frame with $s_{i,j,t}^{cl}$, where $s_{i,j,t}^{cl}$ equals 650 651 to $s_{i,j,t}^{cl} = \left[\cos(c^{cl}, m_{cl}(f_{i,j,t}^{int})) - \delta\right]/\lambda$. c^{cl} represents the concept vector for the *collision* event and m_{cl} is a fullyconnected layer transforming $f_{i,j,t}^{int}$ into the desired space.

5.1.3 Physical Property Inferencer

At the heart of our model, the Physical Property Inferencer 656 (PPI) handles intricate and composite physical interactions 657 by analyzing object motion trajectories extracted from both 658 reference and target videos. The PPI utilizes a graph neural 659 network [55] to predict mass and relative charge for each 660 object pair, where node features capture object-centric prop-661 erties (such as mass), and edge features encode pairwise 662 properties (such as relative charge). The PPI employs a se-663 ries of message-passing operations on the input trajectories 664 of N objects within the video. The process is described by: 665

$$\mathbf{v}_{n}^{0} = f_{emb}(\mathbf{p}_{n}^{t}), \quad \mathbf{e}_{n_{1},n_{2}}^{l} = f_{rel}^{l}(\mathbf{v}_{n_{1}}^{l}, \mathbf{v}_{n_{2}}^{l}), \\ \mathbf{v}_{n_{1}}^{l+1} = f_{enc}^{l}(\sum_{n_{1} \neq n_{2}} \mathbf{e}_{n_{1},n_{2}}^{l}),$$
(2)

Here, $f_{(...)}$ are functions implemented by fully-666 connected layers. We then use two fully-connected layers 667 to predict the output mass label $f_v^{pred}(\mathbf{v}_i^2)$ and edge charge 668 label $f_e^{pred}(\mathbf{e}_{i,j}^1)$, respectively. Notably, the PPI is not trained 669 in a fully-supervised manner but is optimized via leverag-670 ing the gradients from differentiable question answering. 671 The complete physical property of a set of videos can be 672 represented as a fully connected property graph, where 673 each node corresponds to an object that appears in at least 674 one video within the set. Meanwhile, each edge indicates 675 whether the connected nodes possess the same, opposite, 676 or no relative charge (i.e. it signifies whether one or both 677 objects are charge-neutral). In Figure 4, we illustrate that the 678 physical property inferencer (PPI) independently predicts 679 the objects' properties in each reference video, covering 680 only part of the property graph. To align predictions across 681 different nodes and edges, we utilize the static attributes of 682 objects identified by the video perceiver. By aggregating the 683 sub-graphs generated from each video in the set through 684 max-pooling over nodes and edge predictions, we obtain 685 the complete object properties graph. 686

5.1.4 Property-based Dynamic Predictor

To predict objects' positions at the t + 1 frame, based on their 688 full trajectories and properties (mass and charge) at the t-689 th frame, we employ a dynamic predictor implemented by 690 graph neural networks. For the *n*-th object at the *t*-th frame, 691 we represent it with $\mathbf{o}_n^{t,0} = ||_{t-3}^t (x_n^t, y_n^t, w_n^t, , h_n^t, m_n)$, using 692 a concatenation of its object location (x_n^t, y_n^t) , size (w_n^t, h_n^t) 693 and the mass prediction (m_n) by the Physical Property 694 inferener over a history window of 3. By incorporating a 695 history of object locations rather than solely relying on the 696 location at the *t*-th frame, we encode object velocity and 697 accommodate for perception errors. Specifically, we have 698

$$\mathbf{h}_{n_{1,n_{2}}}^{t,0} = \sum_{k} z_{n_{1,n_{2},k}} g_{emb}^{k}(\mathbf{o}_{n_{1}}^{t,0}, \mathbf{o}_{n_{2}}^{t,0}),
\mathbf{o}_{n_{2}}^{t,l+1} = \mathbf{o}_{n_{2}}^{t,l} + g_{rel}^{l} \left(\sum_{\substack{n_{1} \neq n_{2} \\ n_{1}}}^{n_{1} \neq n_{2}} (\mathbf{h}_{n_{1},n_{2}}^{t,l}) \right),
\mathbf{h}_{n_{1,n_{2}}}^{t,l+1} = \sum_{k} z_{n_{1,n_{2},k}} g_{enc}^{k,l} ([\mathbf{o}_{n_{1}}^{t,l+1}, \mathbf{o}_{n_{1}}^{t,0}], [\mathbf{o}_{n_{2}}^{t,l+1}, \mathbf{o}_{n_{2}}^{t,0}]),$$
(3)

where the variable $k \in (0, 1, 2)$ represents whether the two connected nodes carry the same, opposite, or no relative 700

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charge. The k-th element of the one-hot indication vector 701 $\mathbf{z}n_1, n_2$ is denoted as $\mathbf{z}_{n_1, n_2, k}$. The message-passing steps 702 are indicated by $l \in [0,1]$ and functions $g_{(...)}$ are im-703 plemented through fully-connected layers. For predicting 704 object location and size in the (t + 1)-th frame, we em-705 ploy a function comprising a single fully-connected layer, 706 707 $g_{pred}(\mathbf{o}_{n_2}^{t,2})$. To forecast future frames for predictive questions, we initialize the dynamic predictor with the last three 708 frames of the target video and iteratively predict subsequent 709 frames by feeding the generated predictions back into the 710 model. For counterfactual queries, we use the first three 711 frames of the target video as input, updating the predicted 712 objects' mass labels (m_i) and the corresponding one-hot 713 indicator vector $\mathbf{z}_{i,j}$ accordingly, to obtain physical predic-714 tions with counterfactual properties labels. 715

5.1.5 Differentiable Symbolic Executor 716

The differentiable symbolic executor first adopts a program 717 parser [6], [56] to transform the input question into a se-718 ries of program operations. The program parser is trained 719 in a fully-supervised manner as in [5], [6]. The executor 720 then executes the symbolic operations on the latent object-721 centric representation derived from the other modules and 722 the output of the final operator serves as the solution to 723 the question. We adopt a probabilistic approach, similar 724 725 to the methodology proposed in [7], to represent the object states, events, and results of all operators during the 726 training phase. This probabilistic representation allows for a 727 differentiable execution process, considering the latent rep-728 resentations derived from both the observed and predicted 729 scenes. As shown in the dotted lines of Figure 4, it becomes 730 feasible to optimize the video perceiver, visible property 731 grounder, physical property inferencer, and property-based 732 dynamic predictor within the symbolic execution procedure. 733

5.2 Training Mechanisms 734

The proposed PCR features multiple functional modules, 735 and optimizing these modules presents great challenges due 736 to several factors: 1) the lack of dense property annotations 737 738 for both visible concepts and hidden physical properties, 2) the complexity of physical properties and their interaction 739 with other visible properties, and 3) fewer training exam-740 ples compared to the previous physical reasoning dataset 741 CLEVRER. To address these challenges, we propose two 742 novel training mechanisms for model optimization: 1) Cur-743 riculum Learning for Physical Reasoning in Section 5.2.1, 744 and 2) Learning by Imagination in Section 5.2.2. 745

5.2.1 Curriculum Learning for Physical Reasoning 746

We design a novel curriculum learning mechanism to op-747 timize the PCR introduced in Section 5.1. We first train a 748 program parser to parse the question and answers into ex-749 ecutable programs with a sequence-to-sequence model [56]. 750 In lesson 1, we filter out and select the factual questions 75 without physical property description to learn an initial 752 model to ground visible properties like colors, shapes, and 753 754 *collisions*. In lesson 2, we include all the factual questions to teach the model to infer objects' physical properties with 755 the physical property inferencer. During this lesson, we 756 align the objects' dynamics in different videos and property 757

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predictions with the static visible property label prediction 758 from lesson 1. In lesson 3, we utilize the property prediction 759 results from the last lesson as pseudo labels to train a 760 property-based dynamic predictor, which predicts objects' dynamics in the counterfactual and predictive scenes. Finally, we fine-tune all components in an end-to-end manner with all question-answer pairs from the training set. 764

5.2.2 Learning by Imagination

One key challenge for the PCR on the ComPhy dataset is 766 the complexity of its video scenarios compared to previous 767 datasets like CLEVRER [2], which has 152,572 question-768 answer pairs, while ComPhy has only 55,764 pairs but 769 with more variances in physical property variances. To 770 improve the training efficiency, we introduce a new train-771 ing mechanism, named Learning by Imagination. Specifically, 772 when a counterfactual question states "Which event would 773 happen if the purple object were heavier?", it implicitly indicates 774 that "there is a purple object" and "the purple object is not 775 *heavy*". These implicit statements can be transformed into 776 executable programs to enhance the learning of both the vis-777 ible property grounder and the physical property inference 778 introduced in Section 5.1.2. Note that the ability to learn and 779 reason in counterfactual situations is a hallmark of human 780 thought [57], [58]. 781

5.3 Performance Analysis

Effectiveness of Physical Property Inference. We com-783 pare the proposed PCR with the previous neuro-symbolic 784 method CPL [5] in table 5. We can see that the PCR performs 785 better on all kinds of questions compared to the baseline 786 methods in Table 3. This shows the effectiveness of neuro-787 symbolic models for physical reasoning. Second, although 788 our PCR has no reliance on physical property labels and 789 visual attribute labels during training, it can achieve compa-790 rable performance to the previous model CPL that requires 791 dense annotation for videos on factual questions. 792

One distinguished advantage of PCR over end-to-end 793 models [41], [43] is it enables step-by-step investigations and 794 thorough analysis for physical concept learning in videos. 795 We compare the model prediction from the PCR with the 796 ground-truth labels and calculate the accuracy. Table 7 lists 797 the result. We found that our model could effectively grasp 798 visible concepts like "colors", "moving" and "collisions". We 799 also notice that the physical property inferencer in PCR 800 can achieve reasonable accuracy on physical concepts like 801 "mass" and "charge". which shows PCR is able to learn phys-802 ical properties from objects' trajectories and interactions. 803 However, we also notice the performance gap between the 804 hidden physical properties and the visible properties, which 805 indicates that the bottleneck of the performance on factual 806 questions lies in the hidden physical property inference. 807 Effectiveness of Dynamics Reasoning. We further compare 808 our PCR with CPL and its variant CPL-DPI for dynamic rea-809 soning in table 5. CPL-DPI follows the previous model NS-810 DR [6] to adopt dynamic particle interaction networks [59] 811 (DPI) for dynamic prediction. Note that DPI adopts graph 812 neural networks for dynamic prediction without consider-813 ing the variance of physical properties. Compared CPL and 814 PCR with CPL-DPI, we can see the importance of modeling 815

Methods	Factual	Prec	lictive	Count	erfactual	Methods	Factual	Prec	lictive	Count	erfactual
		per opt.	per ques.	per opt.	per ques.			per opt.	per ques.	per opt.	per ques.
CPL-DPI [59]	-	73.3	50.8	61.1	16.6	PCR w/o R	68.7	52.0	28.1	54.9	28.0
CPL [8]	80.5	75.3	56.4	68.3	29.1	PCR w/o CI	70.3	51.2	24.4	54.0	28.0
PCR	76.0	80.0	62.0	70.0	29.0	PCR	78.3	75.0	56.5	70.5	50.2

TABLE 5: Evaluation of PCR on the test set of ComPhy. TABLE 6: Ablation study of PCR on the validation set of The best performance is in boldface. ComPhy. The best performance is in boldface.



Fig. 5: A qualitative example of PCR on ComPhy. The left-up blue box shows the original video and a counterfactual question to answer. The right half table shows the executable program sequence parsed from the question with concepts related to it and outputs after execution. Specifically, the left-down chart illustrates the execution process of PCR for the program "counterfact charge": 1. PCR utilizes a PPI to parse factual charge properties of objects in the scene; 2. PCR modifies their properties according to the counterfactual concept and predict new dynamics using a dynamic predictor.

Methods	Static Attributes D		Static Attributes Dynamic Attributes Event				nts	Physica	l Properties	
	Color	Shape	Material	Moving	Stationary	In	Out	Collision	Mass	Charge
PCR w/o R	91.0	91.8	92.8	83.3	85.2	85.6	81.8	86.8	79.5	45.0
PCR w/o CI	91.9	89.1	94.0	82.6	84.9	86.3	81.4	89.0	80.8	44.8
PCR	96.3	96.8	97.1	81.5	86.0	85.5	70.3	88.0	86.8	68.1

TABLE 7: Evaluation of video concept learning on the validation set.

mass and charges on nodes and edges of the graph neural 816 networks for dynamic prediction. Moreover, compared with 817 CPL, PCR achieves better performance on predictive ques-818 tions and performs competitively on counterfactual ques-819 tions, which shows the effectiveness of the differentiable 820 executor for the optimization of property-based dynamic 821 predictor, physical property inference, and visible property 822 grounder. The performance of our approach surpasses that 823 of the baselines listed in table 3, particularly in counter-824 factual and predictive questions. This achievement demon-825 strates the model's capability to predict the movements of 826 objects in counterfactual and future scenarios, based on the 827

identification of their underlying physical properties.

Furthermore, our evaluation in Section 4.2 highlights a 829 noticeable disparity between the performance of our model, PCR, and human performance, particularly in the domain of counterfactual reasoning. We observed that PCR's dynamic predictor still exhibits limitations when it comes to long-term dynamic prediction. This indicates that further enhancements to the dynamic predictor could potentially yield even higher performance improvements for PCR.

Ablation Study. We conduct a series of ablation studies to 837 prove the effectiveness of the PCR in table 6 and table 7. PCR 838 w/o R denotes learning the property model without using 839

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reference videos. PCR w/o CI denotes the model without 840 counterfactual imaging. We want to answer the following 841 questions. We report the question-answering accuracy in 842 table 6 and the concept classification accuracy in table 7. 843 Comparing with PCR w/o R and PCR, we can see that 844 845 reference videos provide important information for concept identification especially for the physical properties, mass and 846 *charge* in table 7 and constantly improve question-answering 847 performance in different kinds of questions. Comparing 848 PCR w/o CI and PCR, we can see that the counterfactual 849 imaging mechanism in Section 5.2.2 can improve the mod-850 els' abilities in physical property identification in table 7, 85 showing its effectiveness to learn physical reasoning. 852

More Diverse Physical Simulated Scenes. To better evalu-853 ate the model's performance on diverse physical scenes, we 854 have simulated a diverse set of ComPhy dataset. The diverse 855 set introduces 13 distinct object categories—including items 856 such as mugs, pots, chairs, and more-in contrast to the 857 primitive shapes used in the original benchmark. In addi-858 tion, we incorporate 9 varied backgrounds with realistic textures and lighting conditions, and increase the total number 860 of possible question-answer pairs to 175. The new objects 861 span a wider range of shapes and material properties. These 862 enhancements allow for a richer set of physical interactions, 863 enabling the simulation of complex, compositional events.

We have also conducted new experiments on these new 865 scenes, and the performance results can be seen in Table 8. 866 From the table, we have the following observations. First, 867 we can see that our model (PCR) still constantly outper-868 forms the other baselines, showing the effectiveness of using 869 neuro-symbolic models for physical reasoning. Second, we 870 also observe that the average model performance is worse 871 than their accuracy on the original data in Table 3 and 872 Table 5. We believe that the reason is that the new physical 873 scenes have provided more diverse physical interaction 874 among the objects, making it more challenging for the AI models. We have also conducted a human study similar 876 to the original ComPhy paper. The accuracy for different 877 kinds of questions is 88.6 for factual questions, 73.7 for 878 predictive questions, and 78.9 for counterfactual questions, 879 much better than existing models in Table 8. This shows 880 that although the scenes become more diverse, people can 881 still handle these questions well. We provide more details 882 883 on diverse simulated videos in the supplementary material. Generalization to Real-World Scenes. We evaluated the 884 performance of our new model, PCR, on the real-world 885 dataset. It achieved 63.5% accuracy on factual questions, 70.4% on predictive questions (per option), 62.7% on predic-887 tive questions (per question), 54.6% on counterfactual ques-888 tions (per option), and 36.5% on counterfactual questions 889 (per question). From Table 4, PCR consistently outperforms 890 the MAC model across all question types, demonstrating its 89 enhanced effectiveness in physical reasoning. 892

Qualitative Case Study. As shown in Figure 5, PCR can transfer the question query into a series of executable operators, perceive objects' visible properties, infer objects' physical properties, and predict their corresponding dynamics to correct answer the question. Note that such step-bystep investigation is not possible in previous end-to-end models like MAC and ALOE, showing the transparency and interpretability of our PCR.

Methods	Factual	Prec	lictive	Counte	erfactual	
		per opt.	per ques.	per opt.	per ques.	
Random	1.8	50.1	22.9	48.1	24.0	
Frequent	15.7	50.0	0.0	50.0	0.0	
Blind-LSTM	43.2	50.3	25.0	49.2	23.2	
CNN-LSTM [40]	49.6	52.8	29.9	55.7	29.7	
HCRN [41]	51.5	56.3	34.1	51.9	30.1	
MAC [42]	51.7	50.4	28.9	51.9	26.3	
ALOE [43]	46.9	52.4	29.0	51.5	28.6	
CNN-LSTM (Ref) [40]	49.7	51.4	23.3	55.6	30.5	
MAC (Ref) [42]	50.6	51.9	33.3	50.8	25.2	
ALOE (Ref) [43]	48.6	51.2	26.1	52.9	27.2	
ALPRO [44]	47.1	51.8	28.9	52.6	28.4	
GPT-40-mini [9]	42.5	50.0	29.2	58.8	30.7	
Gemini [10]	34.2	50.3	25.7	49.4	30.6	
PCR (ours)	68.4	58.3	34.9	60.3	32.8	
Human Performance	88.6	82.9	73.7	88.2	78.9	

TABLE 8: Evaluation of physical reasoning on ComPhy-DIV. Human performance is based on sampled questions. See the text for more details. **Red** text and **blue** text indicate the first and second best results other than human performance.

5.4 Discussion on Intergrate PCR with LVLMs

Combining PCR with LVLMs offers a powerful paradigm 902 for enhancing both robustness and flexibility. First, LVLMs 903 can replace or augment the program parser in PCR via 904 in-context learning, improving program synthesis for di-905 verse linguistic formulations. Second, LVLMs' broad world 906 knowledge can be invoked through a dedicated large lan-907 guage model-based module to handle commonsense rea-908 soning tasks that lie outside PCR 's original training dis-909 tribution. Finally, LVLMs can act as high-level controllers, 910 orchestrating PCR 's neural modules alongside external 911 modules to seamlessly tackle novel tasks. This integration 912 leverages the precise, learned functionality of PCR and the 913 generalist capabilities of LVLMs, yielding a more versatile 914 and powerful system. We provide more experiments and 915 analysis of integration of PCR and LVLMs in the supple-916 mentary material. 917

6 CONCLUSIONS

In this paper, we introduce the Compositional Physical Rea-919 soning benchmarks, which challenge models to infer hidden 920 physical properties such as mass and charge from limited 921 video observations and leverage this information to predict 922 dynamics and answer structured questions. Our evaluation 923 of state-of-the-art models on ComPhy reveals substantial 924 limitations in their ability to reason about these hidden 925 attributes. We also propose a neuro-symbolic framework, 926 PCR, that integrates object-centric representations with 927 modular reasoning to jointly learn and infer both visible 928 and hidden physical properties. We further present a real-929 world dataset to evaluate the generalization of physical rea-930 soning models beyond simulation. Our findings highlight 931 the critical role of hidden physical properties in dynamic 932 scene understanding and expose the gap between current 933 model capabilities and human-level reasoning, paving the 934 way for more robust and generalizable physical reasoning 935 in AI systems. 936

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